

Detection of COVID-19 in noisy X-ray images using learning-to-augment incorporated noise-robust deep CNN

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Abstract

Deep convolutional neural networks (CNNs) are used for the detection of COVID-19 in X-ray images. The detection performance of deep CNNs may be reduced by noisy X-ray images. To improve the robustness of a deep CNN against impulse noise, we propose a novel CNN approach using adaptive convolution, with the aim to ameliorate COVID-19 detection in noisy X-ray images without requiring any preprocessing for noise removal. This approach includes an impulse noise-map layer, an adaptive resizing layer, and an adaptive convolution layer to the conventional CNN framework. We also used a learning-to-augment strategy using noisy X-ray images to improve the generalization of a deep CNN. We have collected a dataset of 2,093 chest X-ray images including COVID-19 (452 images), non-COVID pneumonia (621 images), and healthy ones (1,020 images). The architecture of pre-trained networks such as SqueezeNet, GoogleNet, MobileNetv2, ResNet18, ResNet50, ShuffleNet, and EfficientNetb0 has been modified to increase their robustness to impulse noise. Validation on the noisy X-ray images using the proposed noise-robust layers- and learning-to-augment strategy-incorporated ResNet50 showed 2% better classification accuracy compared with state-of-the-art method.

Keywords: Convolutional neural network, impulse noise, X-ray image classification, adaptive convolution, COVID-19.

33 **1. Introduction**

34 ***1.1. Detection of COVID-19 in X-ray Images***

35 Coronavirus disease 2019 (COVID-19) has a devastating effect on public health,
36 industry, and global economy. One major need to fight the pandemic is to have the ability to
37 detect COVID-19 cases early, such as via the chest X-ray image examination. Prior studies
38 suggest that chest X-ray images have beneficial diagnostic features as adjuvant diagnostic tool
39 in COVID-19 compared to RT-PCR and can be useful to detect and initiate treatment early
40 [1]. Deep learning algorithms such as deep convolutional neural networks (CNNs) previously
41 demonstrated great promise in various disease diagnosis, often better than expert clinicians [2].
42 Thus, detection of COVID-19 in chest X-ray images using deep learning can also be used as a
43 potential tool for evaluating and monitoring COVID severity [1-6].

44 ***1.2. Classification of X-ray Images using CNN***

45 A CNN is an effective tool for image classification, which has been used in various fields
46 such as health, economics, and agriculture [4-8]. Last year, various types of CNNs were
47 extensively used in COVID-19 detection in medical images. For example, to detect COVID-
48 19 in chest X-ray and computed tomography (CT) images, Jia et al. [2] used two variants of
49 CNN, namely, improved-MobileNet and improved-ResNet. These deep CNNs were designed
50 to dynamically combine features from different layers, a property that the baseline MobileNet
51 and ResNet lacked. The improved-MobileNet has been used in the detection of COVID-19,
52 viral and bacterial pneumonia (i.e., non-COVID pneumonia), and healthy images. Likewise,
53 the improved-ResNet has been employed to discriminate COVID-19, non-COVID pneumonia,
54 and healthy images. These approaches achieved an accuracy of 99.6% on chest X-ray images
55 and 99.3% on the CT images. Thakur et al. also used deep CNN on X-ray images to detect
56 COVID-19 [9]. This model was trained for binary classification on a database of X-ray images,
57 containing 1,917 COVID-19 and 1,960 healthy cases. This method achieved a classification
58 accuracy of 99.64%, F-measure of 99.59%, and receiver operating characteristics (ROC) of
59 100%. Munusamy et al. designed a CNN architecture by combining the Fractal blocks and U-
60 Net [10] to classify X-ray images [11], and demonstrated better classification performance
61 compared to state-of-the-arts such as ResNet50 [12], Xception [13], and InceptionResNetV2
62 [14]. In addition, their model was easily trainable on chest X-ray images. An ensemble model
63 of ResNet50 Error Correcting Output Code (ECOC) was developed by Pathan et al. for the
64 detection of COVID-19 in chest X-ray images [15]. The ensemble model included CNNs,

65 which were optimized using Grey Wolf Optimizer [16] and Whale Optimization [17]. They
66 achieved a multiclass classification accuracy of 98.8%, when the model classified chest X-ray
67 images among COVID-19, healthy, and viral pneumonia cases. Mostafiz et al. proposed a
68 hybrid method of CNN and discrete wavelet transform to detect COVID-19 in chest X-ray
69 images [18]. After a preprocessing operation of X-ray image enhancement and segmentation,
70 image features were extracted by deep CNN and discrete wavelet transform. Afterwards, the
71 optimum features with minimum redundancy and maximum relevance were selected via the
72 recursive feature elimination process. Finally, a random forest-based bagging method was used
73 for the COVID-19 detection task, which demonstrated a classification accuracy of 98.5%.

74 **1.3. Impulse Noise in X-ray Images**

75 Chest X-ray images often get corrupted by the impulse (salt and pepper) noise [19-24].
76 This corruption is typically caused by a malfunctioning X-ray receiver, bit errors in X-ray
77 image transmission, and faulty memory locations in hardware. The impulse noise corrupts pixel
78 intensities in a X-ray image, causing the corrupted pixel having either the maximum or
79 minimum gray level value. The bipolar impulse noise is defined as:

$$80 \quad , \quad (1)$$

81 where denotes the intensity of an impulse noise-corrupted pixel in a X-ray image. If ,
82 intensity will be seen as the brightest dot on the X-ray image and will be seen as the
83 darkest dot. On the other hand, if either or , then the noise is of unipolar type. Finally,
84 if , then the impulse noise will be similar to salt and pepper having a randomly distributed
85 value. When the impulse noise reduces the quality of X-ray images considerably, detection of
86 COVID-19 in the corrupted X-ray image becomes difficult. To address this problem, Lu et al.
87 developed a method for impulse noise removal using a weighted neighbor pixel-based gain
88 factor adaption [19]. In this method, all pixels in a selected window are sorted and grouped
89 based on the gray level variation. After grouping the pixels, the median value and distribution
90 ratio are calculated for each group to estimate the values of the gain factors. These gain factors
91 eventually are used as wights for neighboring pixels that replace the noise-corrupted pixel.
92 Using a fuzzy switching median filter and the concept of information sets, Arora et al.
93 introduced a filter to remove the impulse noise from images [23]. This method works in two
94 phases: the first phase detects pixels corrupted by the impulse noise, and the second phase
95 operates the filter on noisy pixels using an adaptive switching criterion. Satti et al. proposed an

96 impulse noise removing filter using min-max average pooling technique [22]. This approach
97 showed an increase in peak signal to noise ratio (PSNR) of 1.2 dB in the restored medical
98 images compared to the noisy counterparts. The classification performance of a CNN gets
99 deteriorated, when input images are corrupted by the impulse noise [25]. Preprocessing input
100 images to remove noise before feeding to a CNN usually improves the classification
101 performance of the CNN. However, state-of-the-art filtering-based noise removing approaches,
102 discussed above, are often time- and computation-intensive.

103 **1.4. Proposed Method**

104 To increase the robustness of a CNN to the impulse noise, we propose a novel CNN
105 framework including a built-in noise-map layer, an adaptive resizing layer and an adaptive
106 convolution layer. We summarize our technical contributions as:

- 107 1. We introduce a noise-map layer module in the CNN framework that generates a binary
108 noise-map indicating the spatial location of noisy and normal pixels in an image, which
109 ultimately helps to improve the task performance of a CNN by letting it avoid the noisy
110 pixels during training. This module also helps to avoid preprocessing of images to remove
111 noise.
- 112 2. We also introduce an adaptive image resizing module in the CNN framework that can
113 simultaneously resize an image and remove noise from at the front end of a CNN.
- 114 3. Further, we introduce an adaptive convolution layer module that incorporates the noise-
115 map from the first module into the convolution estimation function, which helps to
116 effectively shut off remaining noisy pixels in the input image.
- 117 4. We show the efficacy of the proposed deep CNN framework on clinical X-ray images of
118 COVID-19, non-COVID pneumonia and healthy subjects.

119 The remainder of this paper is structured as follows. We describe our dataset in Section 2. In
120 Section 3, we detail the novel components of a CNN. Extensive experimentation and
121 corresponding results are discussed in Section 4. The conclusion is presented in Section 5.

122 **2. Data**

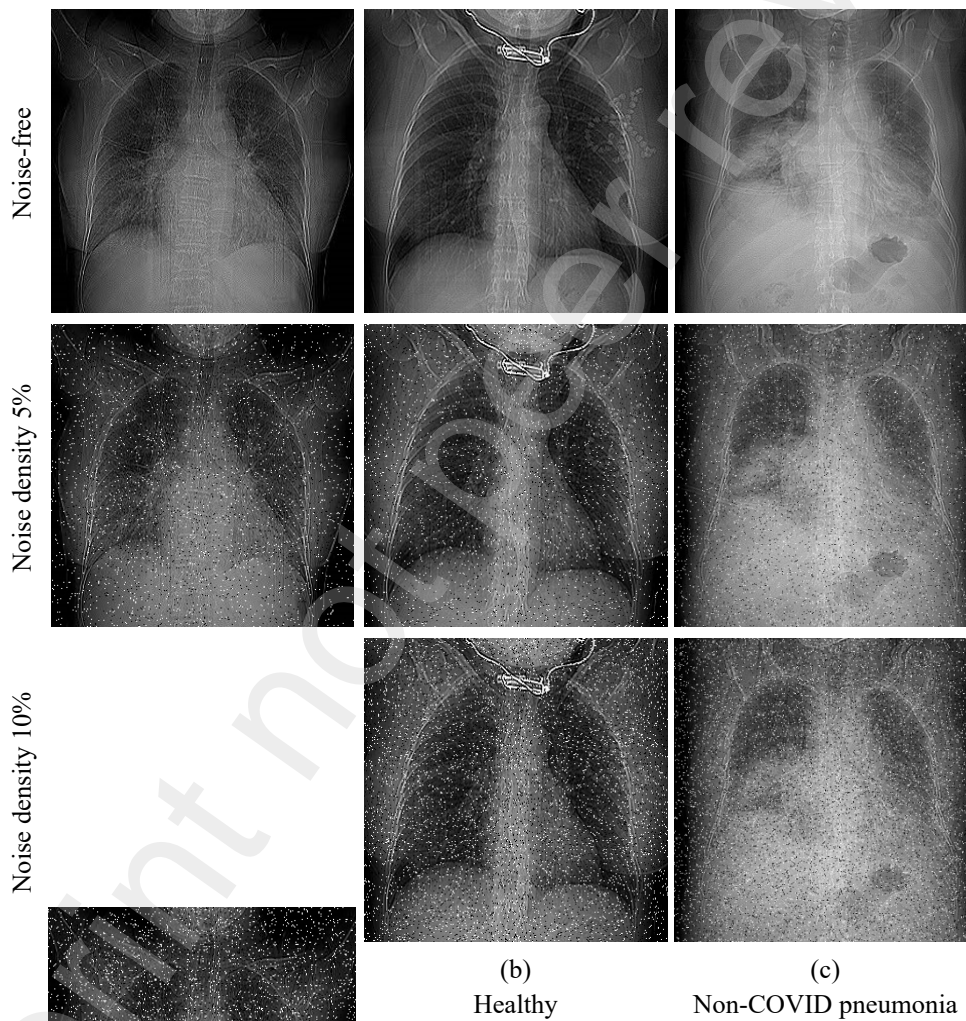
123 We accessed a database of 2,093 chest X-ray images in the Esfarayen University of
124 Medical Science, Esfarayen, Iran. Table 1 summarizes the patients' diagnoses. All the X-ray
125 images were in Joint Photographic Experts Group (JPEG) file format. We resized all X-ray
126 images to a common input size for the pre-trained CNNs (i.e., SqueezeNet, GoogleNet,
127 MobileNetv2, ResNet18, ResNet50, ShuffleNet, and EfficientNetb0). We show samples of

128 collected chest X-ray images (noisy and noise-free) for COVID-19, healthy, and non-COVID
 129 pneumonia cases in Figure 1.

130 **Table 1: Summary of Patients' Diagnoses.**

Diagnosis	Number of subjects/patients	Data collection timeline (years)
COVID-19	452	2020-2021
Non-COVID pneumonia	1,020	2018-2021
Healthy	621	2018-2021

131



132 **Figure 1: Chest X-ray images of (a) COVID-19, (b) healthy, and (c) non-COVID**
 133 **pneumonia cases. The first row contains the noise-free images. The second and**
 134 **third rows contain images with the noise density of 5% and 10%, respectively.**

135

136 **3. Methodology**

137 In this section, detection of COVID-19 in noisy X-ray images using noise-robust deep
 138 CNN based on adaptive convolution is presented which classifies impulsive noisy images
 139 without any preprocessing for noise removal. Figure 2 illustrates the general process of the
 140 proposed method for detection of COVID-19 in noisy images.

141 **3.1. Impulse Noise Detection**

142 The pixels corrupted by the impulse noise can be detected using the analysis of local
 143 statistical properties of an image. In this paper, we use a switching technique-based fuzzified
 144 degree [26] to detect noise-free and noisy pixels in an image. Figure 3 illustrates the pipeline
 145 of 4-step noise detection procedure.

146 **Step 1.** Let W denotes a selected processing window, which is a small patch of the corrupted
 147 image centered at location (x, y) . The size of the processing window is $W \times W$ pixels. The processing
 148 window is further divided into $w \times w$ pixels overlapped sub-windows (see Figure 4).

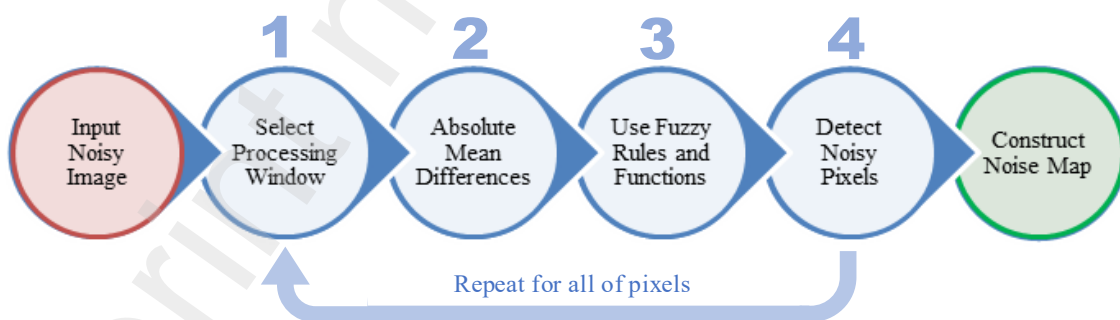
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Figure 2: The schematic diagram of the proposed method.

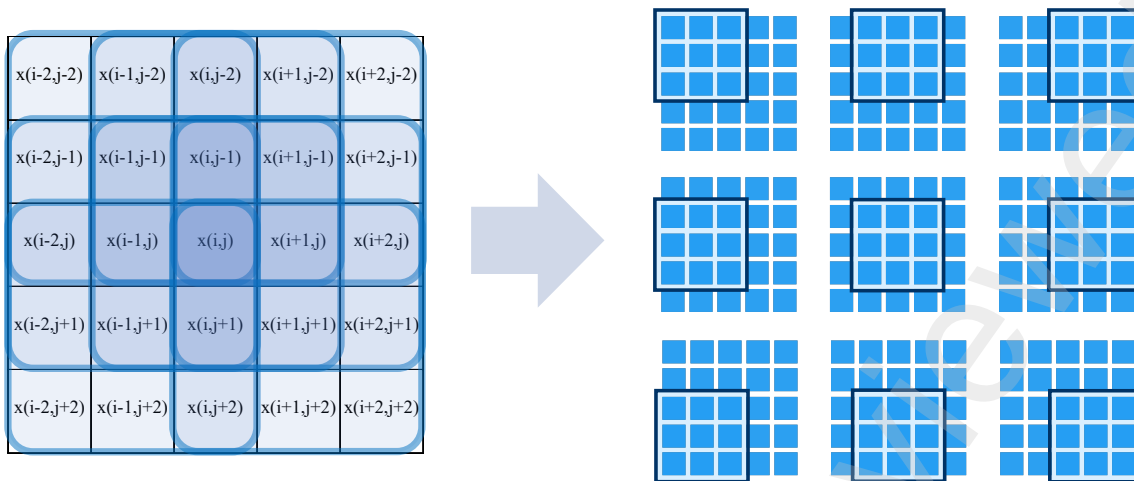
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154
155

Figure 3: The 4-step pipeline of noise detection using the analysis of local statistical properties of an image [26].

156



157 **Figure 4: The pixels processing window is divided into pixels overlapped sub-windows.**

158 **Step 2.** In this step, we calculate the absolute mean differences. Let w_k indicates sub-window
 159 for k . Medians of nine sub-windows are estimated as [26]:

160
$$\text{Median}(w_k) \quad (2)$$

161 These median values of nine sub-windows (in equation 2) are put in ascending order as [26]:

162
$$\rightarrow \text{Median}(w_k) \quad (3)$$

163 The absolute mean differences are then calculated as:

164
$$\text{AMDF} = \frac{1}{9} \sum_{k=1}^9 |\text{Median}(w_k) - \text{Median}(w_{k+1})| \quad (4)$$

165
$$\text{AMDF} = \frac{1}{9} \sum_{k=1}^9 |\text{Median}(w_k) - \text{Median}(w_{k+1})| \quad (5)$$

166 where, AMDF and $\text{Median}(w_k)$ are employed to determine noisy pixels of the image.

167 **Step 3.** In this step, we used fuzzy logic to detect if the current pixel is noisy or noise-free. To
 168 do this, we assign the degree of impulsiveness to each pixel by using fuzzy gradient values
 169 [26]. To distinguish noisy pixels from edges, the difference between the gradients is
 170 classified into nondeterministic features (μ or ν). Figure 5 shows the fuzzy membership
 171 functions μ and ν that represent fuzzy set μ and fuzzy set ν , respectively. The fuzzy
 172 membership functions are defined as [26]:

173
$$\mu(x) = \frac{x - a}{b - a} \quad (6)$$

174
$$\nu(x) = \frac{b - x}{b - a} \quad (7)$$

175 , (8)

176 (9)

177 (10)

178 (11)

179 where τ_1 and τ_2 are threshold parameters. The fuzzy membership degree is defined as [26]:

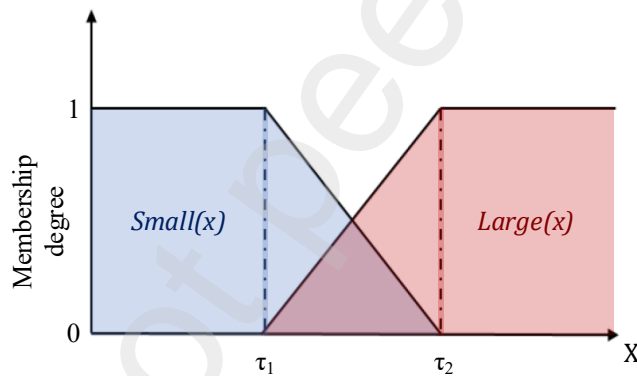
180 (12)

181 **Step 4.** In the fourth step, the switching technique based fuzzified degree [26] is applied to
 182 detect the noisy pixels. As shown in Figure 6, if $\mu_{Small}(x) > \mu_{Large}(x)$, the interrogated pixel is noise-free.

183 Otherwise, the interrogated pixel is noisy. Thus, a noise-map, $N(x)$ can be defined as:

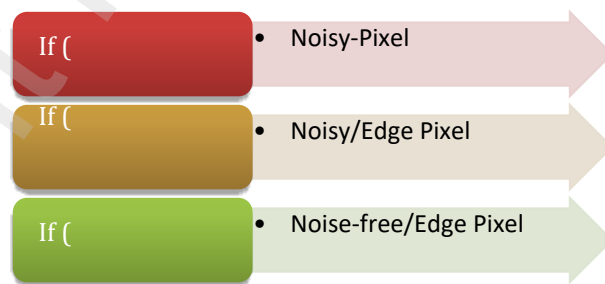
(13)

184 where x is the location of the interrogated pixel. The noise-map $N(x)$ for a whole image is
 185 then constructed by examining all the pixels in that particular image using the above-mentioned
 186 technique.



187

188 **Figure 5: Fuzzy membership functions 'Small(x)' or 'Large(x)'.**



189

190 **Figure 6: Noise detection rules.**

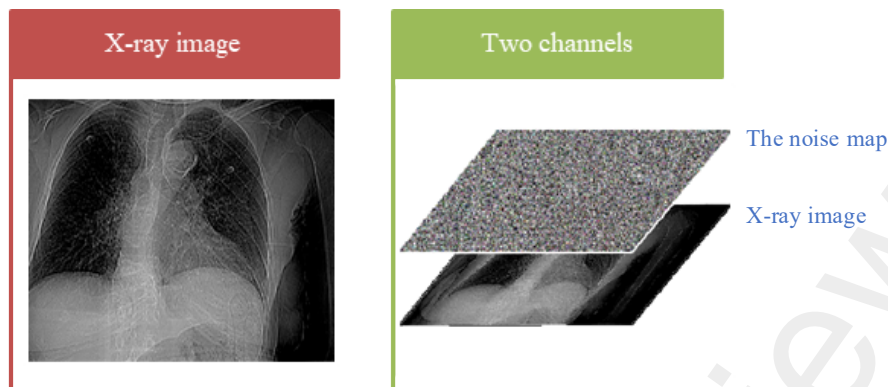


Figure 7: Two channels for each image.

In this paper, to make our CNN framework robust to impulse noise, we use the estimated noise map as the second channel for the corresponding X-ray image, when fed to the CNN. As shown in Figure 7, each image contains two channels: noise-map channel, grayscale X-ray channel.

3.2. Adaptive Resizing

All input images to a CNN (e.g., GoogleNet, MobileNetv2, ResNet18, ResNet50, ShuffleNet, EfficientNetb0, etc.) usually have a common dimension (e.g., pixels). Also, if a model is pretrained, the dimension of the input images during finetuning should match to the dimension of the images on which the model is pretrained. Since the models we use in this paper are pretrained, we need to resize our X-ray images so that their dimension matches to the dimension of the images used in pretraining. In this paper, rather than using a conventional interpolation-based image resizing approach, we adopted an adaptive image resizing approach, which is more robust on noisy images. To illustrate the mechanism of this resizing approach, we demonstrate resizing two pixels noisy images with low and high noise density, respectively, to pixels noise-reduced images in Figure 8. In the first step, an image is divided into blocks for subsampling (Figure 8b). We can see in Figure 8c that if the pixel value in the resized image is taken from the central pixel of the corresponding block, then noisy pixel values from the original image are easily passed to the resized image. To avoid this issue, we adopt the adaptive resizing [25] technique, where noisy pixel values do not get passed to the resized image (Figure 8d). After resizing images using corresponding noise-maps, we also resize the noise-maps so that the updated noise-map size matches the updated image size. Assuming that w is a set of candidate pixels to resize in the selected sub-window, updated noise-maps are obtained using following.

If (all of pixels in w is noisy) then

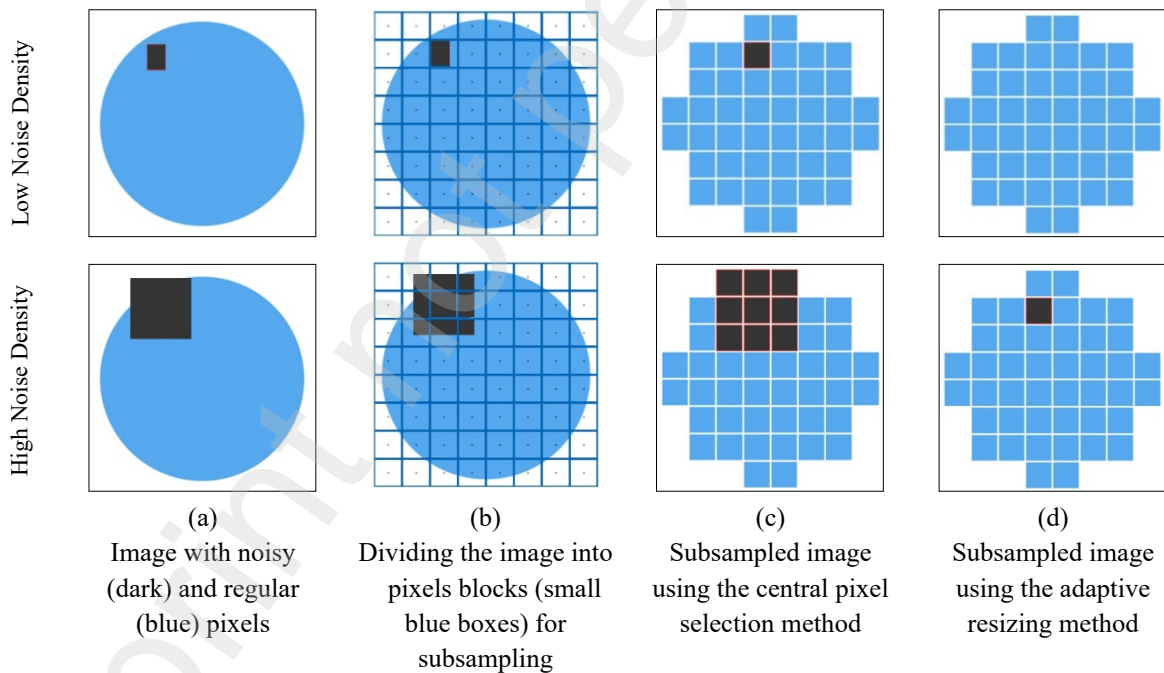
```

Set the corresponding coordinates of updated noise-map to noisy.
Else
Set the corresponding coordinates of updated noise-map to non-noisy.
End if

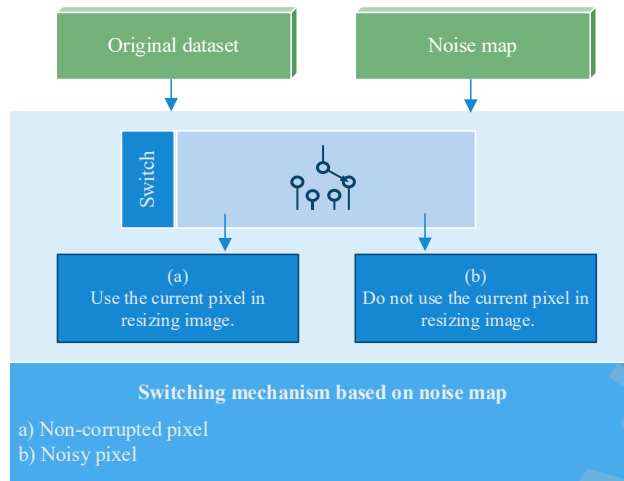
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215 This adaptive pixel selection works by eliminating noisy pixels in reducing the image
216 size and makes the noisy pixels are not participated in the process of X-ray image dimension
217 reduction.

218 In this study, we incorporated this adaptive resizing function as a layer in the CNN
219 framework to increase its robustness to noisy X-ray images. In the proposed adaptive resizing
220 layer, an original noisy X-ray image (e.g., pixels) is resized to pixels by using the
221 information of the spatial distribution of noise, derived from the corresponding noise-map
222 (discussed in Section 3.1). Using this adaptive resizing layer in our CNN framework, as shown
223 in Figure 9, we can avoid the transmission of noisy pixels from the original X-ray image to the
224 resized X-ray image. Figure 10 illustrates the pipeline of our adaptive image resizing at the
225 front end of the CNN.
226

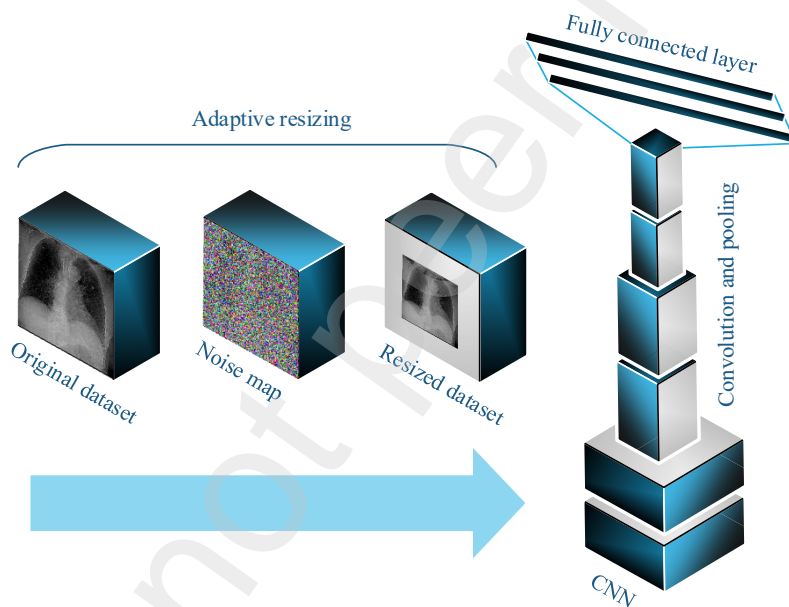


227 **Figure 8: Comparison of image resizing techniques using the central pixel selection and**
228 **adaptive pixel selection (i.e., adaptive resizing).**
229



230
231

Figure 9: The architecture of the adaptive resizing layer [25].



232
233

Figure 10: The pipeline of adaptive resizing operation at the front end of the CNN.

234 **3.3. Adaptive Convolution**

235 After adaptive resizing (discussed in Section 3.2), there still might exist noisy pixels in the X-
 236 ray images (second row of Figure 8d). Therefore, we design our convolution layer adaptive to
 237 make it more robust to image noise. Typically, a new feature map is generated by a
 238 convolution layer of a CNN as [27]:

$$239 \quad (14)$$

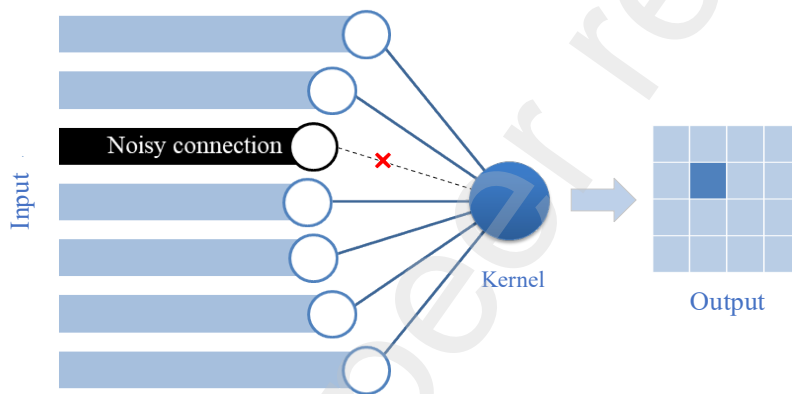
240 where \mathbf{y}_k is the location coordinate of the k^{th} kernel, \mathbf{x} is the input image/feature patch,
 241 \mathbf{W}_k is the learned weight matrix of the k^{th} convolution kernel, and \mathbf{b}_k is the bias of the convolution

242 layer. In this paper, we modify the conventional convolution layer of a CNN to make it more
 243 robust to noise by incorporating our noise-map as [25]:

244
$$\dots$$
 (15)

245 Since noise-map s is a binary map, incorporating it into the convolution kernel helps not to
 246 propagate noisy pixel value forward along the network. We illustrate this operation in Figure
 247 11, where we see that the noisy pixels get shut off (i.e., having a value of 0) during feature
 248 calculation. Figure 12 illustrates the architecture of the adaptive convolutional layer for
 249 robustness of deep CNN to noisy X-ray images. Eliminating noisy connections avoids inputting
 250 impulsive noisy pixels to the next layers.

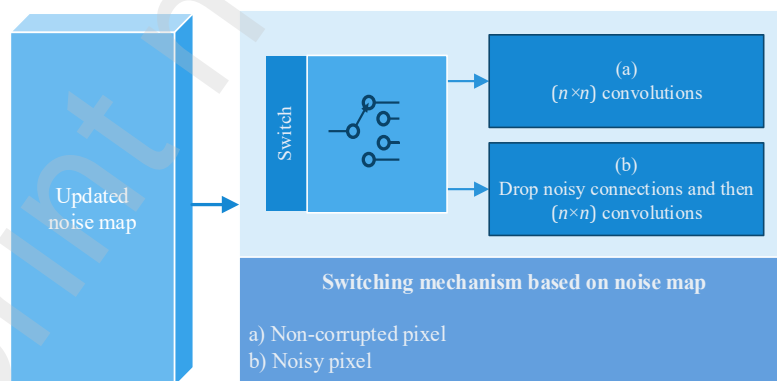
251



252

253 **Figure 11: Schematic diagram illustrating the shutting off a noisy pixel during convolution**
 254 **operation in a CNN convolution layer.**

255



256

257 **Figure 12: The architecture of the proposed noise-robust adaptive convolution layer.**

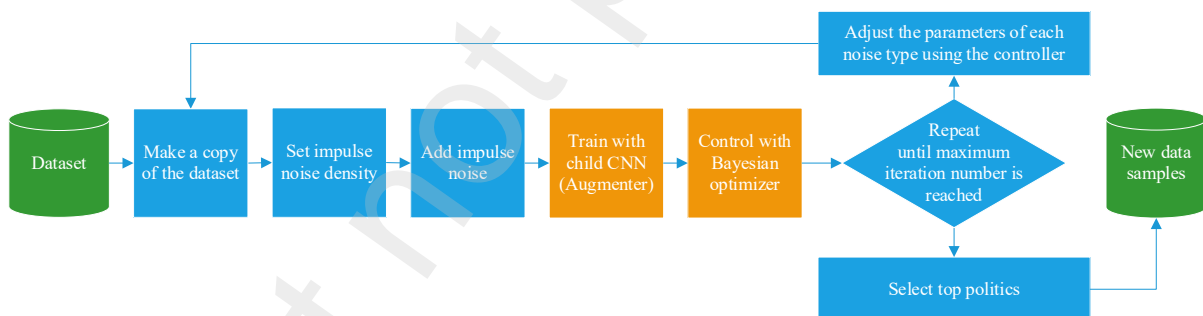
258 **3.4. Learning-to-Augment Using Noisy Data**

259 Adding some noise to data (e.g., the impulse noise, the Gaussian noise) is a strategy for
 260 data augmentation [8]. We have employed a learning-to-augment strategy [8] using noisy X-

261 ray images to generate the new data. The noise density () is the parameter of impulse noise
 262 [28-30] and the mean () and variance () are parameters of the Gaussian noise [31, 32]. As
 263 shown in Figure 13, the learning to augment using noisy data is composed of a noisy data
 264 generator, a controller, an augments, and child models. Firstly, the original dataset is
 265 partitioned into two folds. Then a noisy data generator adds impulse noise and Gaussian noise
 266 to the X-ray images in each fold, separately. The augmenters generate new X-ray images based
 267 on the parameters that the Bayesian optimizer has found. Then, each fold is separately fed to
 268 the child CNN models. Using the output of child CNNs, the controller increases performance
 269 of weak policies and keeps improved policies. The controller employs the Bayesian
 270 optimization algorithm to optimize augmentation policies (the parameters of impulse noise and
 271 Gaussian noise). Assuming that is the search space and is the loss function of a child CNN,
 272 the Bayesian optimization algorithm can be defined as [8]:

$$(16)$$

274 The optimizer algorithm in equation 16 obtains that minimizes for in a bounded domain
 275 . The final loss function of the Bayesian optimization algorithm is composed of the individual
 276 loss values from child CNNs. The optimization process lasts until the optimized parameters is
 277 achieved.



279
 280 **Figure 13: Flowchart of learning-to-augment using noisy data.**

281 4. Implementation Details

282 In this section, we discuss details of our extensive experimental setup in detecting
 283 COVID-19 in noisy X-ray images. We divided our X-ray dataset into training (70%), validation
 284 (10%), and test (20%) sets as shown in Table 2. We also list the types of CNNs (i.e.,
 285 conventional CNN or noise-robust CNN) used during training, validation, and testing in Table
 286 3. We used learning-to-augment strategy using noisy data only in the training and employed
 287 the proposed noise-robust method only in the testing phase. This overall strategy ensures that

our model learns from both noise-free and noisy data. Learning-to-augment strategy using the noisy X-ray images starts by setting the impulse noise density. The noisy data generator creates X-ray images corrupted by the impulse noise. Bayesian optimization algorithm finds the optimum data augmentation policy (i.e., the impulse noise density, ρ), where AlexNet [27] is used as the backbone. The Bayesian optimizer found the optimal value of ρ to be 22%.

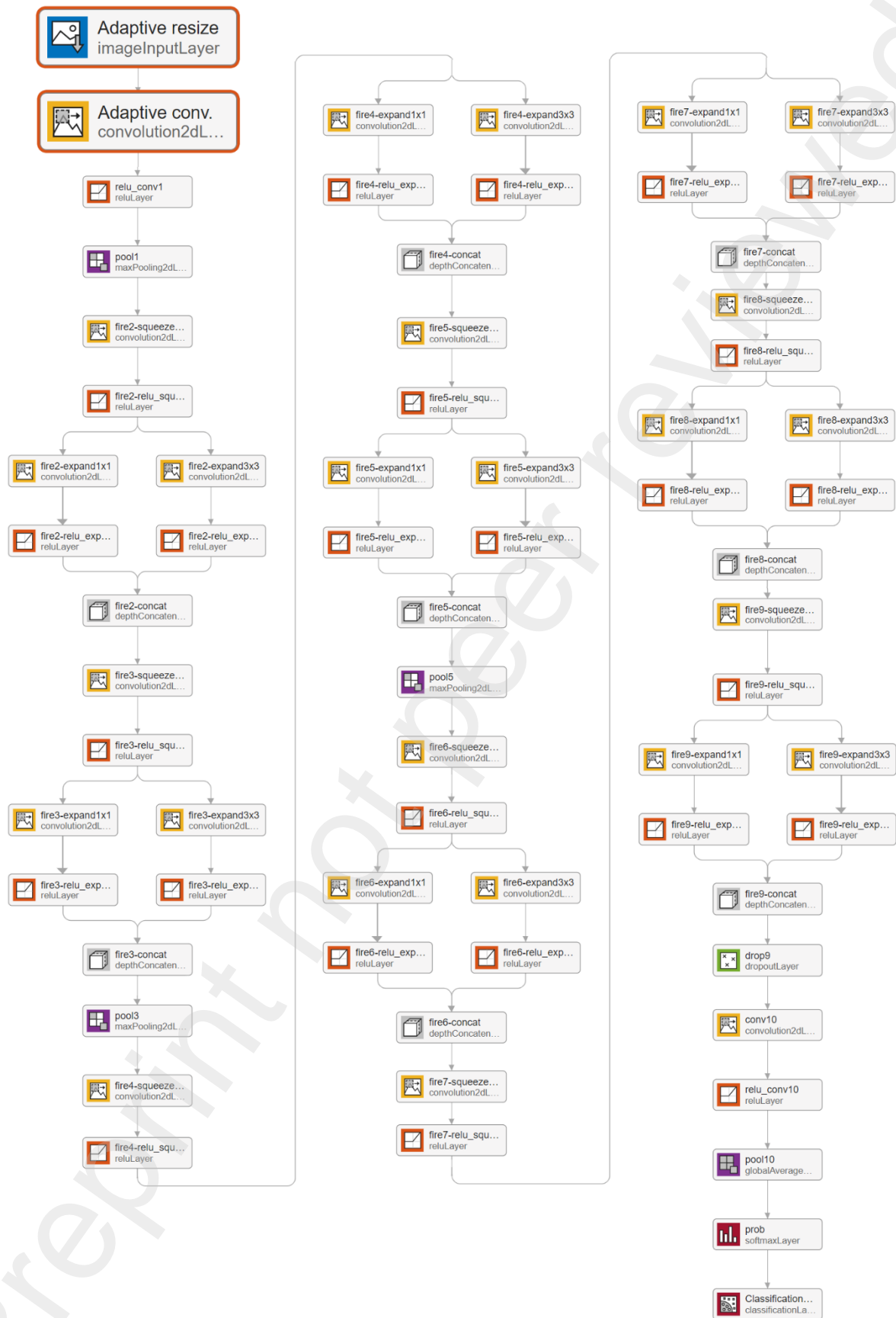
Table 2: Data partitioning for training, validation, and testing in this study.

Phase	Data splitting	# of original images	# of augmented images	Total # of images
Train	70%	1,466	1,466	2,932
Validation	10%	209	-	209
Test	20%	418	-	418

Table 3: Types of CNNs (conventional/noise-robust) used in training, validation, and testing.

Phase	Type of CNN	# of noise-free images	# of noisy images	Total # of images
Train	Conventional CNN	1,466	1,466	2,932
Validation	Conventional CNN	209	-	209
Test	The noise-robust CNN	-	418	418

We incorporated our proposed noise-robust modules in the state-of-the-art networks such as SqueezeNet [33], GoogleNet [34], MobileNetv2 [35], ResNet18 [12], ResNet50 [12], ShuffleNet [36], and EfficientNetb0 [37]. As an example, Figure 14 and Table 4 show the architecture and configuration of our proposed model using pre-trained SqueezeNet, respectively, for the classification of X-ray images. We can see in Figure 14 and Table 4 that the SqueezeNet model takes input through the proposed adaptive resizing layer that resizes an X-ray image from $W \times H$ pixels to $w \times h$ pixels, where new interpolated pixel values are estimated from the noise-free neighboring pixels in the original image. Also, in the first convolutional layer, the convolution kernel incorporates the binary noise-map so that noisy pixel values of the input images do not propagate to the next layer. Similarly, the adaptive resizing layer is incorporated in other deep CNNs (GoogleNet, MobileNetv2, ResNet18, ResNet50, ShuffleNet, and EfficientNetb0) to robustify those to impulse noise as well. Also, the first convolution layer of all the networks were modified to incorporate the adaptive convolution to make those robust to noise. It is also worth noting that the size of the original X-ray images in our dataset is larger than the usual input image size of pre-trained deep CNNs. Consequently, after performing adaptive resizing, an input image usually becomes less noisy before it is fed to the adaptive convolution layer.



313
314

Figure 14: The architecture of the proposed noise-robust SqueezeNet model.

Table 4: The configuration of the proposed noise-robust SqueezeNet model.

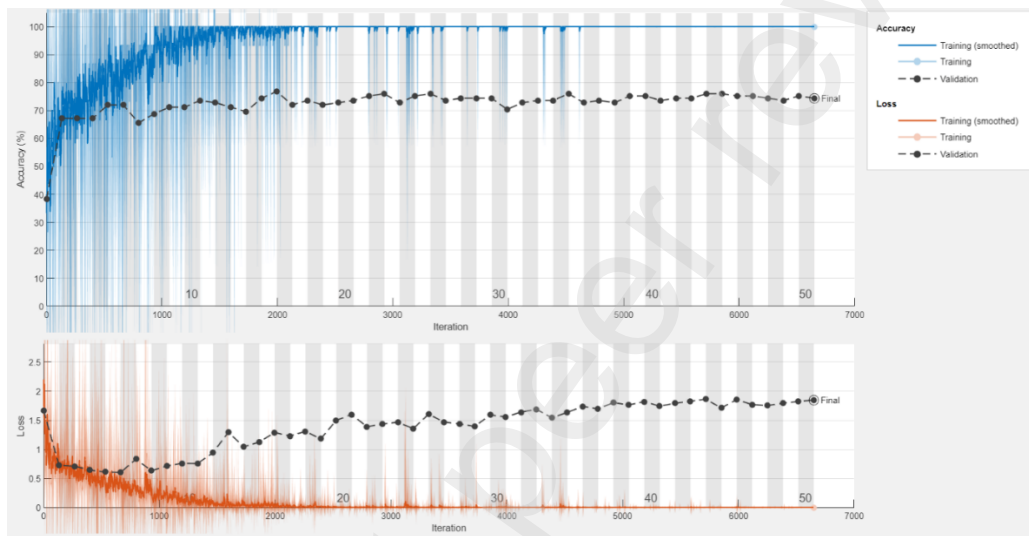
#	Type	Descriptions	#	Type	Descriptions
0	Adaptive Resizing	512×512×3 images	35	Convolution	48 1×1 convolutions stride [1 1] and padding [0 0 0 0]
1	Input of Image and Noise-Map	227×227×3 images with 'zerocenter' normalization	36	ReLU	
2	Adaptive Convolution	64 3×3 convolutions stride [2 2] and padding [0 0 0 0]	37	Convolution	192 3×3 convolutions stride [1 1] and padding [1 1 1 1]
3	ReLU		38	ReLU	
4	Max Pooling	3×3 max pooling stride [2 2] and padding [0 0 0 0]	39	Convolution	192 1×1 convolutions stride [1 1] and padding [0 0 0 0]
5	Convolution	16 1×1 convolutions stride [1 1] and padding [0 0 0 0]	40	ReLU	
6	ReLU		41	Concatenation	Depth concatenation of 2 inputs
7	Convolution	64 1×1 convolutions stride [1 1] and padding [0 0 0 0]	42	Convolution	48 1×1 convolutions stride [1 1] and padding [0 0 0 0]
8	ReLU		43	ReLU	
9	Convolution	64 3×3 convolutions stride [1 1] and padding [1 1 1 1]	44	Convolution	192 1×1 convolutions stride [1 1] and padding [0 0 0 0]
10	ReLU		45	ReLU	
11	Concatenation	Depth concatenation of 2 inputs	46	Convolution	192 3×3 convolutions stride [1 1] and padding [1 1 1 1]
12	Convolution	16 1×1 convolutions stride [1 1] and padding [0 0 0 0]	47	ReLU	
13	ReLU		48	Concatenation	Depth concatenation of 2 inputs
14	Convolution	64 3×3 convolutions stride [1 1] and padding [1 1 1 1]	49	Convolution	64 1×1 convolutions stride [1 1] and padding [0 0 0 0]
15	ReLU		50	ReLU	
16	Convolution	64 1×1 convolutions stride [1 1] and padding [0 0 0 0]	51	Convolution	256 3×3 convolutions stride [1 1] and padding [1 1 1 1]
17	ReLU		52	ReLU	
18	Concatenation	Depth concatenation of 2 inputs	53	Convolution	256 1×1 convolutions stride [1 1] and padding [0 0 0 0]
19	Max Pooling	3×3 max pooling with [2 2] and padding [0 1 0 1]	54	ReLU	
20	Convolution	32 1×1 convolutions stride [1 1] and padding [0 0 0 0]	55	Concatenation	Depth concatenation of 2 inputs
21	ReLU		56	Convolution	64 1×1 convolutions stride [1 1] and padding [0 0 0 0]
22	Convolution	128 3×3 convolutions stride [1 1] and padding [1 1 1 1]	57	ReLU	
23	ReLU		58	Convolution	256 1×1 convolutions stride [1 1] and padding [0 0 0 0]
24	Convolution	128 1×1 convolutions stride [1 1] and padding [0 0 0 0]	59	ReLU	
25	ReLU		60	Convolution	256 3×3 convolutions stride [1 1] and padding [1 1 1 1]
26	Concatenation	Depth concatenation of 2 inputs	61	ReLU	
27	Convolution	32 1×1 convolutions stride [1 1] and padding [0 0 0 0]	62	Concatenation	Depth concatenation of 2 inputs
28	ReLU		63	Dropout	50% dropout
29	Convolution	128 3×3 convolutions stride [1 1] and padding [1 1 1 1]	64	Convolution	1000 1×1 convolutions stride [1 1] and padding [0 0 0 0]
30	ReLU		65	ReLU	
31	Convolution	128 1×1 convolutions stride [1 1] and padding [0 0 0 0]	66	Pooling	Global Average Pooling
			67	Softmax	
			68	Classification	Output

316

Table 5: Properties of the pretrained CNN models we used in this study.

Network	Depth	Size	Parameters (Millions)	Input Image Size
SqueezeNet	18	5.2 MB	1.24	227 227
GoogleNet	22	27 MB	7.00	224 224
MobileNetv2	53	13 MB	3.50	224 224
ResNet18	18	44 MB	11.70	224 224
ResNet50	50	96 MB	25.60	224 224
ShuffleNet	50	5.4 MB	1.40	224 224
EfficientNetb0	82	20 MB	5.30	224 224

317



318

319 **Figure 15: Accuracy vs. iteration and Loss vs. iteration curves for the training and validation**
 320 **of GoogleNet.**

321 We ran our deep learning experiments using the deep learning toolbox of MATLAB
 322 2021a in an Intel(R) Core(TM) i7-7700HQ CPU 2.81 GHz with 32 GB of RAM, and Nvidia
 323 GTX 1070 GPU with 8 GB VRAM. We employed stochastic gradient descent (SGD) with a
 324 learning rate of 0.001 to finetune the pretrained CNNs. In Table 5, we show a summary of the
 325 properties of CNNs we used in our study.

326 5. Comparison of Time Complexity

327 The run-time of the methods that improve the quality of noisy X-ray images is of great
 328 important [38], especially for the point-of-care machines in the clinical environment. Typically,
 329 X-ray images corrupted by the impulse noise are enhanced in two phases [22, 39, 40]. In the
 330 first phase, noise-free or noisy pixels are identified. Then in the final phase, enhancement of
 331 the quality of X-ray images is done. Following the same workflow, we do noise detection by

332 generating the noise-map of an X-ray image by using a switching technique-based fuzzified
333 degree in the first phase of our proposed method. Afterwards, as a manifestation of the second
334 phase, we design our CNN such that it becomes robust to noise and does not require any
335 preprocessing of an X-ray image in terms of noise reduction.

336 Recent works [41-44] suggested that the median filtering is one of the fastest method of
337 removing the impulse noise. However, the time complexity of computing the median filter
338 kernel by quick sort algorithm is $O(n \log n)$. In contrast, the proposed model does not require to sort
339 the data, rather it uses the switching technique with time complexity of $O(n)$ to identify noisy
340 pixels. Thus, the comparison of time complexity between the proposed method and the median
341 filtering (i.e., one of the fastest method for removal of impulse noise [41-44]) indicates the
342 superiority of the proposed method.

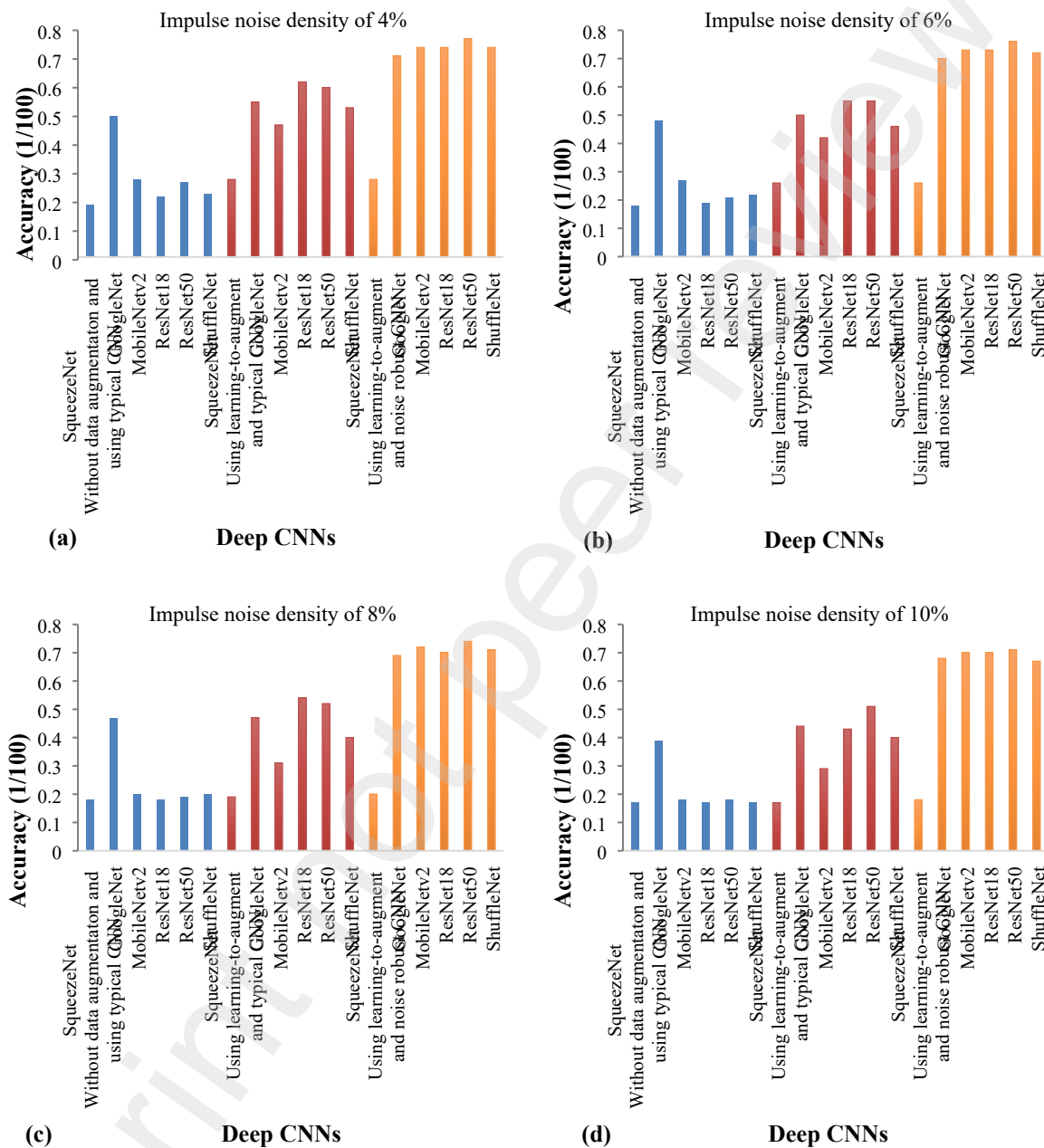
343 **6. Experimental Results**

344 In this section, we discuss the performance comparison of the proposed approach with
345 respect to the state-of-the-arts on the detection of COVID-19 in noisy X-ray images. The
346 COVID-19 detection accuracy curves during GoogleNet training and validation with the
347 impulse () noise-corrupted X-ray images are illustrated in Figure 15. We compare the
348 classification performance by the proposed method to that of the state-of-the-art methods in
349 three scenarios: (i) training conventional CNNs using data without augmentation, (ii) training
350 conventional CNNs with data augmented by learning-to-augment strategy, and (iii) training
351 proposed noise-robust CNNs with data augmented by learning-to-augment strategy. Figure 16
352 illustrates the COVID-19 detection performance for the test X-ray dataset corrupted by impulse
353 noise with of 4%, 6%, 8%, and 10% for all three scenarios. It can be seen that the COVID-19
354 detection accuracy by the pretrained networks using scenario-iii is the best among all three
355 scenarios.

356 We also show the COVID-19 detection errors (i.e., CNN classification error) on the
357 impluse noise-corrupted X-ray testset for in three scenarios. We see in Table 4 that the
358 performance by the ResNet50 in scenario-iii is the best among other error performances. It
359 reduced the error in scenario-iii compared to scenario-ii by 2% (i.e., 31% to 29%), and
360 compared to scenario-i by massive 53% (i.e., 82% to 29%) for . Thus, it is clear from Table 4
361 that our proposed approach using adaptive resizing, adaptive convolution, and learning-to-
362 augment strategy has great efficacy in accurately classfying noisy image data. Finally, we show
363 the line charts of COVID-19 detection accuracy using the impulse noise-corrupted X-ray data

364 with for three scenarios. We see in Figure 17 that the scenario-iii showed the best detection
 365 performance among all three scenarios. Thus, it becomes more evident that the proposed
 366 method can effectively classify noisy images with higher accuracy.

367
 368



369 **Figure 16: The accuracy of COVID-19 detection by different methods for noisy X-ray images**
 370 **corrupted by the impulse noise with (a) , (b) , (c) , and (d) .**

371

372 **Table 4: COVID-19 detection error (1/100) on X-ray images corrupted by the impulse noise with . Here,**

373 scenarios: (i) training conventional CNNs using data without augmentation, (ii) training
 374 conventional CNNs with data augmented by learning-to-augment strategy, and (iii) training
 375 proposed noise-robust CNNs with data augmented by learning-to-augment strategy

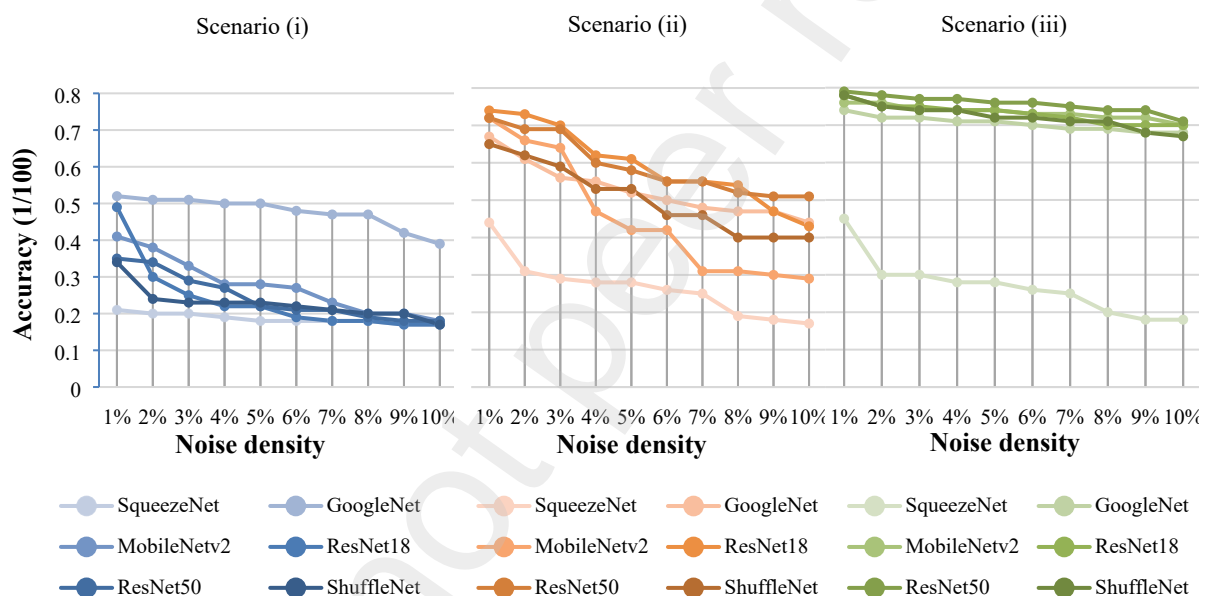
Networks	Scenario	Impulse noise density									
		1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
SqueezeNet	i	0.79	0.80	0.80	0.81	0.82	0.82	0.82	0.82	0.83	0.83
	ii	0.56	0.69	0.71	0.72	0.72	0.74	0.75	0.81	0.82	0.83
	iii	0.55	0.70	0.70	0.72	0.72	0.74	0.75	0.80	0.82	0.82
GoogleNet	i	0.48	0.49	0.49	0.50	0.50	0.52	0.53	0.53	0.58	0.61
	ii	0.33	0.39	0.44	0.45	0.48	0.50	0.52	0.53	0.53	0.56
	iii	0.26	0.28	0.28	0.29	0.29	0.30	0.31	0.31	0.32	0.32
MobileNetv2	i	0.59	0.62	0.67	0.72	0.72	0.73	0.77	0.80	0.80	0.82
	ii	0.28	0.34	0.36	0.53	0.58	0.58	0.69	0.69	0.70	0.71
	iii	0.24	0.24	0.26	0.26	0.26	0.27	0.27	0.28	0.28	0.30
ResNet18	i	0.51	0.70	0.75	0.78	0.78	0.81	0.82	0.82	0.83	0.83
	ii	0.26	0.27	0.30	0.38	0.39	0.45	0.45	0.46	0.53	0.57
	iii	0.22	0.25	0.25	0.26	0.26	0.27	0.28	0.30	0.30	0.30
ShuffleNet	i	0.66	0.76	0.77	0.77	0.77	0.78	0.79	0.80	0.80	0.83
	ii	0.35	0.38	0.41	0.47	0.47	0.54	0.54	0.60	0.60	0.60
	iii	0.22	0.25	0.26	0.26	0.28	0.28	0.29	0.29	0.32	0.33
ResNet50	i	0.65	0.66	0.71	0.73	0.78	0.79	0.79	0.81	0.82	0.82
	ii	0.49	0.49	0.48	0.45	0.45	0.42	0.40	0.31	0.28	0.31
	iii	0.21	0.22	0.23	0.23	0.24	0.24	0.25	0.26	0.26	0.29

376

377 7. Conclusion

378 In this report, we propose a novel noise-robust deep CNN framework for improving
 379 detection of COVID-19 in the impulse noise-corrupted X-ray images. Our proposed framework
 380 includes several novel image processing modules. The noise-map layer module can effectively
 381 improve detection in a noisy image by making use of switching technique based on fuzzified
 382 degree. The adaptive resizing layer module can simultaneously remove noisy pixels while
 383 performing interpolation-based image resizing. In addition, the adaptive convolution layer
 384 module incorporates noise-map from the first module into the convolution operation that
 385 effectively shuts off the remaining noisy pixels in the input image. We further incorporated the
 386 learning-to-augment strategy for automatic augmentation of training images, which improved
 387 the generalizability of the deep models on X-ray images. We incorporated our novel modules
 388 into several pretrained state-of-the-art deep CNNs such as SqueezeNet, GoogleNet,

389 MobileNetv2, ResNet18, ResNet50, ShuffleNet, and EfficientNetb0. Validation of the
 390 proposed noise-robust model on clinically acquired X-ray images from COVID-19, non-
 391 COVID pneumonia and healthy subjects demonstrated better COVID-19 detection
 392 performance on noisy X-ray images compared to the state-of-the-art models. Moreover, the
 393 proposed model requires no preprocessing for impulse noise removal, rather noise removal
 394 happens on-the-fly because of our novel modules, which speeds up the classification of noisy
 395 X-ray. Therefore, our data suggest that the proposed deep CNN framework could be very
 396 effective in classification tasks, even on the noisy data, and could improve the generalization
 397 of deep CNN. In the near future, we aim to examine the ability of our noise-robust CNN to
 398 improve such classification task in the high-density noise-corrupted X-ray images.
 399



400 **Figure 17: Line chart of COVID-19 detection accuracy using the impulse noise-corrupted X-ray**
 401 **data with .**

402
 403
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